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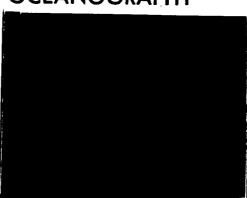
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A GENERAL THEORY OF PERTURBED LIGHT FIELDS, WITH APPLICATIONS TO FORWARD SCATTERING EFFECTS IN BEAM TRANSMITTANCE MEASUREMENTS

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A General Theory of Perturbed Light Fields, With Applications to Forward Scattering Effects in Beam Transmittance Measurements*

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ABSTRACT

The problem of the measurement of the optical properties of a given medium is complicated by the fact that the act of measurement perturbs the distribution of radiant flux in the immediate vicinity of the measuring process. Consequently, the numbers derived from a measurement process do not faithfully reflect the inherent optical properties of the medium under study, but rather contain along with the information sought both the effects of the presence of the measuring apparatus and its characteristic response to radiant flux. The present note contains a general formulation of the equation of transfer for perturbed radiance field in an arbitrary optical medium. The resultant theory is applied to the problem of the measurement of the volume attenuation function.

which take into account the perturbation effect on the light field of the standard measuring apparatus used for the determination of . In addition, the theory provides a means of estimating the relatively elusive forward

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scattering value of the volume scattering function, . Finally, two criteria are given for estimating the order of magnitude of the forward scattering effects encountered in beam transmittance measurements.

INTRODUCTION

It is a cardinal axiom of experimental physics that the act of observing a given phenomenon necessarily disturbs the phenomenon under observation. It follows that the "true" nature of the observed is irreversibly obscured by some such disturbance generated by the observer. This axiom holds in particular in the field of experimental radiative transfer. An important illustration of this is afforded by the experimental procedures followed in the determination of the volume attenuation function α . By way of introduction to the present approach, the classical procedures for finding α will be briefly outlined. The general theory of a perturbed light field is then formulated and applied to the case of the determination of α , which results in the perturbed light field counterparts to the classical procedures. The theory yields five distinct approaches to the problem of the determination of α , each of which may be transformed into an experimental procedure.

The classical procedures for determining of assume that the light field is unperturbed as the probing for the relevant information goes on.

By ignoring the perturbations the investigator is rewarded with analytical formulations of ohm-law simplicity. The price for this is paid by having the resulting prediction curve pass unconcernedly through an array of non-conformist data points. The two main techniques now in use may be classified as the bright-target and dark-target techniques.

Figure 1 depicts the essential geometrical elements of each technique.

In the bright-target technique, T is a self-luminous target viewed by a

Gershun tube (radiance meter) G at a distance r. It is assumed that the target is

angularly small — in fact, of zero solid angular subtense — when viewed at

each point of the path P between T and G. In addition, the effect of the

ambient light field is removed by either a direct shielding of P from its

surrounds or by taking the difference of the G-readings found by turning T

on and then off. The assumption is made that this on-off procedure does not

perturb the ambient light field. Finally, G is assumed to be an ideal

collector: any flux entering G and not on P is not recorded. All these

assumptions combine to reduce the general equation of transfer:

$$dN/dr = -\alpha N + N_* \tag{1}$$

to the particularly simple form

for the radiance along P. Thus if N and N are the inherent and apparent radiances of T along P, then the operation,

$$-\frac{1}{r} \ln \frac{N_r}{N_o} = \infty \tag{2}$$

on the measurable quantities r, N, N is taken to yield the required value of \propto .

The dark-target approach, on the other hand, assigns zero inherent radiance to T. The same assumptions adopted above remain in force. In addition, P is chosen so that N_{*} is constant along P. The solution of (1) leads to the following operation.

$$-\frac{1}{r} \ln \frac{N_2 - N_r}{N_b} = \alpha \tag{3}$$

on the measurable quantities $N_q = N_{\pi}/\alpha$, N_r , and r, and is taken to yield the required value of α .

GENERAL REPRESENTATION OF A PERTURBED LIGHT FIELD

In actuality, the placing of a target T of inherent radiance N_0 in the light field perturbs the light field. Further, the target being a material object occupies a finite volume of space so that it fills a finite subregion $\Xi_+(r')$ of direction space Ξ as viewed at each distance r' on P. From this vantage point, the presence of T causes a perturbation extending over a subset $\Xi_+(r')$ of Ξ . Finally, the Gershun tube, being a material object of finite dimensions, will also contribute its share to the perturbation and, in addition, will record flux entering G which is not strictly on P; the collection of such directions which carry acceptable flux will be denoted in general by $\Xi_S(r')$.

With these observations in mind, the general equation of transfer is transformed to the following exact form for the new context:

$$\frac{dN'(t,\overline{z})}{dt'} = -\alpha(t,N,(t,\overline{z}) + N,(t,\overline{z}) \alpha(t,\overline{z}) \alpha(\overline{z})$$

$$+ \int_{\overline{z}} -\underline{z}^b(t,) \alpha(t,\overline{z}) \alpha(t,\overline{z}) \alpha(t,\overline{z}) \alpha(\overline{z})$$

$$+ \int_{\overline{z}} -\underline{z}^b(t,) \alpha(t,\overline{z}) \alpha(t,\overline{z}) \alpha(\overline{z}) \alpha(\overline{z})$$

$$+ \int_{\overline{z}} -\underline{z}^b(t,) \alpha(t,\overline{z}) \alpha(t,\overline{z}) \alpha(\overline{z}) \alpha(\overline{z})$$

Here, and in the sequel, the symbols N[†], N denote the perturbed and unperturbed radiance functions respectively. The equation may be rewritten more compactly as

$$+ N*(h,\tilde{z}) + N*(h,\tilde{z}) + N*(h,\tilde{z}) = - \sigma_{(h,\tilde{z})} + N*(h,\tilde{z}) + N*(h,\tilde{z})$$

where

$$\alpha'(t') = \alpha(t') - \int_{\Xi_{3}(t')} \sigma(t'; S; S') d\Omega(S'),$$

and

$$N_{*}(r',\underline{s}) = \int_{\underline{x}} N(r',\underline{s}') \, \sigma(r';\underline{s}';\underline{s}) \, d\Omega(\underline{s}').$$

This is the general equation of transfer for a perturbed light field.

Its domain of applicability is quite wide. The notion of Gershun tube is here intended to cover all types of radiance detectors, including such organic

detectors as human eyes. Since all material radiance detectors occupy finite regions in space, they always give rise to a perturbed α , namely the α' of (4). In view of this fact one can raise the question: is it meaningful to talk about a "true α " in <u>practical</u> contexts? Any op rational procedure designed to determine the α of a medium must necessarily be made through the intermediation of a physical recording apparatus. It is, therefore, meaningful to talk or think only about the α' for that instrument, or collection of α' values relative to a given collection of radiance detectors. The "true α' is therefore a constitutive rather than an operational definition, a useful fiction about which one may conveniently cluster for reference the operationally obtainable α' values.

The problem of the determination of α is intimately connected with the determination of the forward scattering values $\sigma_{\bullet}(F') = \sigma(F'; \{; \})$ of the volume scattering function C . Here again the physical limitations of the relevant instruments, in this case the nephelometers, prevent an exact determination of $\sigma_{\bullet}(r')$. Even if the instrument could, by some clever ruse, be forced to look directly down the path to the primary source, what principle will allow the separation of the so-called forward scattered flux from the unscattered transmitted flux? This raises the question: is such an attempted separation meaningful in practice? The answer, clearly, is that it is not. But yet, even with strict experimental justification absent, there appears to be some unavoidable compulsion to conceptually decompose the forward flux. The motivation for such a procedure is apparently an esthetic requirement: one in which the gap in the experimental definition function be closed by the inclusion of the values of the To (+') . The desirability of obtaining α and σ stems from the fact that they are important constitutive constructs which help bring order and completeness into the classification and theoretical study of turbid media. It is with this in mind that the hunt for α and σ_0 is carried out in the sequel.

From the preceding observations, it is seen that even on a phenomenological (or macroscopie) level, the study of light is beset by limitations on the exact experimental determinations of the three basic notions: N, et, and σ . The seeming indeterminacy of N may be side-stepped in principle by defining N operationally as the apparent limit of a sequence $\{N_n\}$ of radiance functions given by a sequence of radiance meters which approaches as a limit the ideal ($\Omega_3 = 0$) radiance meter. The values of et and σ_0 however, are more clusive; their operational definitions are subject, in the sense explained above, to a more fundamental difficulty. Some ways in which this difficulty can be oversome on a practical level are considered below.

LIMEARIZED REPRESENTATION OF SLIGHTLY PERTURBED LIGHT FIELDS

As an illustration of the use of the general representation of a perturbed light field, we reconsider the problem of experimentally determining the volume attenuation function \sim . The discussions which follow apply to arbitrary optical media, e.g., natural hydrosols or aerosols. The equipments used in the classical procedures have been designed so as to minimise, within reasonable limits, the induced perturbations. As a result, relatively small (but yet detectable) perturbations are encountered. A useful feature of these slight perturbations is that they may be represented by certain linearisation conditions imposed on the general structure of (4). We assemble the three conditions for a linearly perturbed light field below:

- (i) The functions $\mathcal{C}(r'; \S; \cdot)$ and $\mathcal{C}(r'; \cdot; \S)$ are constant over $\Xi_{\S}(r')$ and $\Xi_{\S}(r')$, respectively, for each $r', 0 \le r' \le r$. Both have the fixed value $\mathcal{C}_0 \equiv \mathcal{C}(r'; \S; \S)$.
- (ii) $N'(F', \cdot)$ and $N(F', \cdot)$ are constant functions over $\equiv_{\rho}(F')$ for each r', $0 \le F' \le F$, the fixed values will be denoted by N'(F') and N(F') respectively.

(iii) $\equiv_{\rho}(F') = \equiv_{t}(F')$ for each r', $0 \le F' \le F$.

Under these assumptions the general equation (4) is transformed into the following relatively simple structure:

$$\frac{dN'(F')}{dF'} = \left[-\alpha + \sigma_0 \left(\Omega_0(F') + \Omega_1(F') \right) \right] N'(F') - N(F') \sigma_0 \Omega_1(F') + N_*(F'),$$
(5)

where $\Omega_3(r') = \int_{\Xi_3(r')} d\Omega(s)$, $\Xi_k(r') = \int_{\Xi_k(r')} d\Omega(s)$,

the general solution of which is readily obtained:

$$N'(r) = T_r' N'(0) + (T_r')^{-1} \int_0^1 [N_{\pm}(r') - \sigma_0 \Omega_{\xi}(r') N(r')] T_r' dr'$$
(6)

$$T_{\mu}' = \exp\left\{-\alpha r' + \sigma_0 \left[\int_0^r \Omega_3(r'')dr'' + \int_0^r \Omega_4(r'')dr''\right]\right\}. \tag{7}$$

The resulting formulations point the way to several novel measuring techniques for . While the formulations are admittedly approximate in the sense made clear above, they take due cognizance of the major features of a perturbed

light field and the non-ideal character of real Gershun tubes. In this way an essential advance beyond the classical procedures seems possible. Despite the simplified character of the linear theory, its resultant formulations lie just on this side of practical utility. That is to say, within the present experimental framework, the slightest relaxation of the linearizing conditions pushes the resultant theory beyond the borderline of reasonable tractability. However, this observation must be qualified when it comes to using more general approximations based on (4) as a theoretical tool.

APPLICATIONS

Bright-Target Technique

For the case of the bright-target technique, (6) takes a particularly simple form which is based on the following considerations: (i) The realisation of the bright-target technique in practice is in the form of a so-called — meter (a beam-transmittance meter) which consists essentially in the optical system depicted in Figure 2. The most important feature for the present discussion is the condition $\Omega_{5}(r) = \Omega_{4}r$ which this optical system imposes on the two solid angles defined in the general theory. This follows from the effective placement of the source at the focal point of lens A so that the source is essentially imaged on lens B. Thus the solid angle $\Omega_{5}(r')$ (or $\Omega_{4}(r')$) is necessarily the solid angle subtended by the farthest lens from the point r'. (ii) The path P between A and B has been designed so as to be shielded from the surrounding natural light field. From this, it follows that $N_{4}(r') = N(r') = 0$ on P. With these observations, (6) reduces to

so that

$$N'(t)/N'(0) = T_t' = exp \{ - \alpha t' + 2\pi T_0 \phi(t) \}$$
(8)

where

$$\phi(r) = 2\left[\frac{1}{2} - \left(a^2 + r^2\right)^{\frac{1}{2}} + \left(a^2 + \left(\frac{1}{2}\right)^2\right)^{\frac{1}{2}}\right],$$

and where α is the common radius of lenses A and B. For ratios $\alpha/F < 1/10$, (8) may be usefully represented by the approximation

$$T'_{r} = exp\left\{-\kappa r + 2\pi r, \frac{a^{2}}{r}\right\}$$
 (9)

Either (8) or (9) show that the perturbation of the light field leads in this case to an apparently reduced value of \propto as measured by the instrument, e.g., from (9):

$$\alpha' = \alpha - 2\pi\sigma_{\bullet}(\frac{\alpha}{r})^{2}.$$

An apparent reduction of \propto will also be found in the dark-target case. In fact, the general equation for the perturbed light field shows that this apparent decrease in \propto is a universal manifestation traceable directly to the simple fact that for all material Cershun tubes, and all material targets, $\Omega_{\mathbf{q}}(r)$ and $\Omega_{\mathbf{q}}(r)$ are greater than zero.

Dark-Target Technique

In this case the path is chosen so that N_{\pm} and N are constant over its extent. In fact, we set $N_{\pm} = N_{\pm}/a = N$, and N'(0) = 0. $\Omega_{\pm}(F)$ and $\Omega_{\pm}(F)$ are no longer rigidly coupled as in the bright-target case, but now assume the forms:

$$\Omega_{\xi}(r') = 2\pi \left(1 - \frac{r'}{(a^2 + r'^2)^{\frac{1}{2}}}\right)$$

$$\Omega_3(r') = 2\pi \left(1 - \frac{(r-r')}{(b^2+(r-r')^2)^{\frac{1}{2}}}\right),$$

governed by obvious geometrical requirements. Here a, and b are the radii of the target, and photosensitive collecting disk in the Gershun tube, respectively.

Under these conditions, (7) becomes

$$T'_{t'} = e \times \rho \left\{ -\alpha r' + e \pi \sigma_0 \phi(r, r') \right\}, \qquad (10)$$

where

$$\phi(r,r') = 2(r-r') + b - (b^2 + (r-r')^2)^{\frac{1}{2}} - (a^2 + r^2)^{\frac{1}{2}} + (a^2 + r'^2)^{\frac{1}{2}}$$
(11)

and (6) becomes

$$N'(r) = N_1(T_r')^{-1} \int_0^r [\alpha - \sigma_r \Omega_{+}(r')] T_{r'}' dr'.$$
 (12)

The chore of carrying out the integration of (12) can be considerably reduced, and the utility of (12) considerably enhanced, if the following approximate representation of $\phi(r,r')$ is adopted:

$$\phi(r,r') = b - \frac{a^2}{2r} , \qquad (13)$$

which follows from setting

$$2r'-r = -(b^2 + (r-r')^2)^{\frac{1}{2}} + (\alpha^2 + r'^2)^{\frac{1}{2}},$$

$$(\alpha^2 + r^2)^{\frac{1}{2}} = r \left[1 + \frac{1}{2} (\frac{\alpha}{r})^2 \right]^{\frac{1}{2}}.$$

The justification for this may be illustrated by considering a numerical example in which the quantities have magnitudes which are typical for dark-target experiments. Thus let $\alpha/r = b/l = 1/30$, where l = 0.30 meters is the length of the Gershun tube, and r = 10.70 meters. The graphs of Figure 3 show a plot of 2r'-r and the graph it is to approximate.

By means of (13), the form for N'(r) becomes:

$$N'(r) = N_{e} \exp \left[2\pi\sigma_{o} \left(b - \frac{\alpha^{2}}{2r} \right) \right] \left[\left(1 - e^{-\alpha r} \right) - \sigma_{o} \right]_{o}^{r} e^{-\alpha (r-r')} \Omega_{+}(r') dr' \right], \tag{14}$$

which is still a formidable analytical haystack from which one must extract \propto and σ_{\bullet} . Some ways in which this may be done will now be considered.

An Outline of Possible Experimental Procedures

If V_0 is known and ∞ is sought:

Experiment 1. Single use of an & -meter.

Experiment 2. Single dark-target experiment.

If both & and To are sought:

Experiment 3. Two ~-meters used simultaneously.

Experiment 4. Two dark-target experiments conducted simultaneously.

Experiment 5. Simultaneous & -meter and dark-target experiments.

We consider each experiment in turn, but outline only the principle analytical steps required in each case.

Experiment 1. The procedure is straightforward: Knowledge of N'(r)/N'(o) and G, allows an immediate estimate of α from (8), or (9). Fore-knowledge of G, may be obtained by using the G-recovery method.

Experiment 2. Equation (14) may be written as

Experiment 3. Suppose two α -meters, each of having a distinct ϕ -function (equation (8)), simultaneously measure beam transmittance in a given medium. Then, if ϕ_1 , ϕ_2 ; r_1 , r_2 ; and r_1 , r_2 , represent the appropriate quantities of each instrument, the two equations for α and r_0

have the solutions

Preisendorfer, R. W., A New Method for the Determination of the Volume Scatter-Function, Visibility Laboratory report, Index Number NS 714-100, Contract NObs-50274, Scripps Institution of Oceanography, (March, 1956).

Experiment 4. Equation (14) is the basis for this experiment. The general idea is to obtain two readings of N'(r) from two distinct geometrical arrangements, and then solve two simultaneous equations for α and σ . No simple closed expressions for α and σ may be obtained as in Experiment 3. Recourse to numerical solutions is the only way out. The numerical procedure will be considerably simplified if each geometrical arrangement is so made that $b = (a^2/2r) = 0$. This may be done in the following way. Let \mathcal{L} and \mathcal{L} and \mathcal{L} be the effective length and radius of the Gershun tube. Then the radius \mathcal{L} of the dark-target is given by $\mathcal{L} = rbk/\mathcal{L}$, where $k \ge 1$ (i.e., k insures the fulfillment of the condition that the target must at least fill the field of the Gershun tube). Then the condition $b = (a^2/2r) = 0$ requires that the range of the target be $r = 2l^2/b \mathcal{R}^2$.

In illustration, let b/2 = 1/30, 2 = 0.30 meters. Choose two k-values, e.g., $k_1 = \sqrt{2}$, $k_2 = 2$. These numbers now fix a and r for each choice of k:

$$t_1 = 2l^2/bk^2 = 9.00$$
 meters
 $a_1 = t_1bk_1/l = 0.423$ meters
 $t_2 = 4.50$ meters
 $a_2 = 0.300$ meters.

Now returning to (14) in which $b-(\alpha^2/2+)=0$, we have for two such experimental arrangements:

$$C(r_i) = (N_i - N'(r_i))/N_i = e^{-\alpha r_i} + \sigma_0 I(\alpha, \alpha_i, r_i)$$

$$C(r_i) = (N_i - N'(r_i))/N_i = e^{-\alpha r_i} + \sigma_0 I(\alpha, \alpha_i, r_i),$$

where $I(a,a;,r) = \int_{a}^{r} e^{-x(r;-r')} \Omega_{+}(r') dr'$. This set of equations may be rearranged to read:

$$A(\alpha) = \frac{C(r_1) - e^{-\alpha r_1}}{C(r_1) - e^{-\alpha r_1}} = \frac{I(\alpha, \alpha_2, r_1)}{I(\alpha, \alpha_1, r_1)} = B(\alpha).$$

Each side represents a computable function of α (the a_i and r_i being known and fixed during the experiment). Hence both A and B can be graphed over a certain domain of α values. If the curves are graphed over the same set of axes (Figure 4 (b)) the point of intersection of the graphs defines the required α . (The graph of Figure 4 merely represents the idea of this solution procedure; it need not represent an actual set of A and B graphs):

Experiment 5. Equations (8) and (14) are the basis for this experiment.

Equation (8) is solved for σ_o and the resultant expression for σ_o is substituted in (14). After this is done, the remaining procedure is in principle covered by the analytical steps outlined for experiment 2.

Order of Magnitude Estimates

A given bright-or dark-target set up can be given a quick preliminary analysis by means of equations which approximate (8) and (14). The appropriate equation for (8) is given by (9). Turning to (14), we see that a lower bound on the Γ_o -effect may be obtained by setting $\Omega_{\frac{1}{2}}(r') = \Omega_{\frac{1}{2}}(r)$ so that (14) reduces to

$$N'(t) = N_q \exp \left[2\pi \sigma_0 \left(b - \frac{a^2}{2t} \right) \right] \left(1 - e^{-at} \right) \left[1 - \frac{\pi \sigma_0}{a!} \left(\frac{a}{t} \right)^2 \right]. \tag{16}$$

Thus if (16) predicts a measurable deviation from the unperturbed radiance N_q (1- e^{-at}), the actual G-effect produces an even greater deviation (an illustration is given below). Unfortunately, a correspondingly good upper bound is not found in such a simple way, so that no general bracketing expression

can be simply given for N'(+) in the dark-target case. Each problem is best handled separately using (14).

From the preceding analyses it is evident that the &-meter technique appears to be the more simple to handle analytically. From (9) one can estimate the percent difference between & and &':

$$\Delta = 100 \times \frac{\alpha' - \alpha}{\alpha} = -100 \times \frac{2\pi\sigma_0}{\alpha} \left(\frac{\alpha}{r}\right)^2, \quad (17)$$

the minus sign denoting that lpha is always less than lpha .

To gain a rough idea of the order of magnitude of the forward scattering effect in a typical hydrosol and aerosol, we choose for the hydrosol: $\sigma_0 = 1.92/mater$ steradian, $\alpha = 0.402/mater$; and for the aerosol, $\sigma_0 = 9 \times 10^{-4}/mater$ steradian, $\alpha = 32 \times 10^{-5}/mater$. The corresponding values of Δ for a set of α -meters (characterized by their a/r ratios) are given below.

a/r	-∆ (in percent)	
	Aerosol	Hydrosol
1/200	0.044	0.075
1/100	0.176	0.300
1/50	0.704	1.20
1/25	2.82	4.80
1/12,5	11.3	19.2

^{*}The & and G are associated with a wavelength of 478 mu; & and G are based on measurements taken by J. E. Tyler in Lake Pend Oreille, and are representative of moderately clear lake and near-shore ocean water. Depending on the medium, the ratio G/d may range over an order of magnitude. G was estimated using the method of reference 1.

**Based on Waldram's data for industrial haze, as recorded in Middleton, W.E.K., <u>Vision Through the Atmosphere</u>. (Univ. of Toronto Press, 1952), p. 48. G./c. for clear air is on the order of a seventh of that for industrial haze. The associated wavelength is 570 mm. G. was estimated by extrapolation.

We conclude with an example of the use of (16) for the case of the present hydrosol. Using the set-up suggested in Experiment 4, and observing that the path lengths were chosen so that $b-(a^2/2r)=0$, we have:

$$N'(r_1) = N_q e^{\alpha} (1 - e^{-\alpha r_1}) (1 - 0.040) = (0.96) (1 - e^{-\alpha r_1}), r_1 = q_{melos}$$

$$N'(r_1) = N_q e^{\alpha} (1 - e^{-\alpha r_1}) (1 - 0.080) = (0.96) (1 - e^{-\alpha r_1}), r_2 = 4.5 \text{ melos}$$

It appears that a definitely measurable perturbation of the light field would be induced in the present case. Thus, some radical procedure, such as that outlined in Experiment 4, should be followed in order to obtain an accurate estimate of \propto .

SUMMARY

The general equation of transfer for an arbitrarily perturbed light field is formulated (equation (4)). From this is deduced the linearized equation of transfer (5) which is applicable to the study of slightly perturbed light fields such as those induced during the measurement of the volume scattering function or (beam transmittance) by means of the bright-or-dark-target techniques. The general solution (equations (6), (7)) of the linearized equation leads to analytical expressions which may be used to estimate the true value of α when either the bright target approach (equation (8)) or the dark target approach (equation (14)) is used. The general solution of the linearized equation yields in particular five possible experimental procedures leading to an estimate of α . Finally, two methods are given (equations (16), (17)) for estimating the order of magnitude of the forward scattering effects encountered in beam transmittance measurements.

CAPTIONS

Figure 1. Illustrating the geometry of a perturbed light field. T is a generalized target, G represents a Gershun tube (radiance meter). Both T and G induce a perturbation of the radiance distribution about a point P on the path P. In the general case, T need not be on the axis of G. The subregions of direction-space about p which are occupied by the target, the Gershun tube, and the perturbation, are indicated as shown.

Figure 2. The optical system of a typical ω -meter (beam transmittance meter), in particular, one in which $\Omega_{\xi}(t') = \Omega_{\eta}(t')$.

Figure 3. Illustrating an approximation which simplifies the analytical formulation of the dark-tarket technique in typical applications.

Figure 4. Illustrating two numerical procedures for determining \ll .

(a): Experiment 2; (b) Experiment 4; For details, see text.

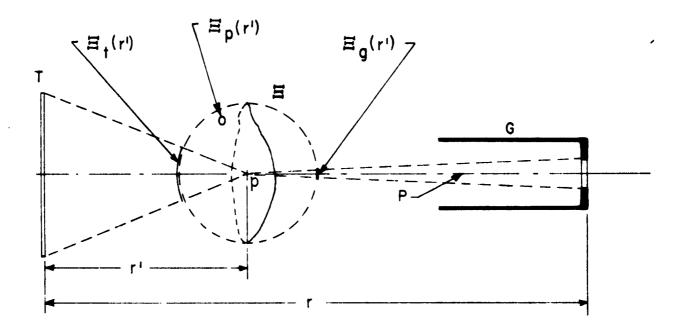


Figure 1
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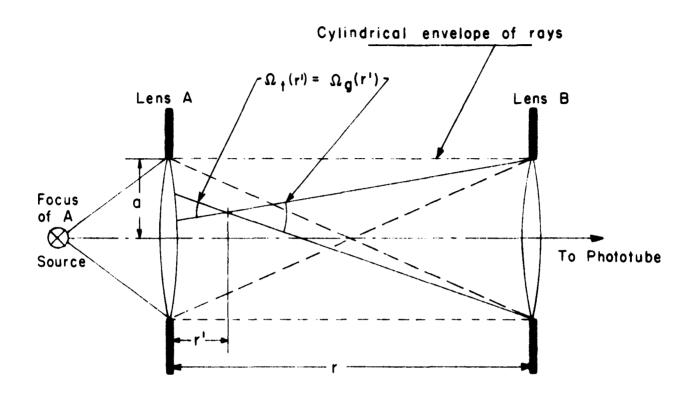


Figure 2
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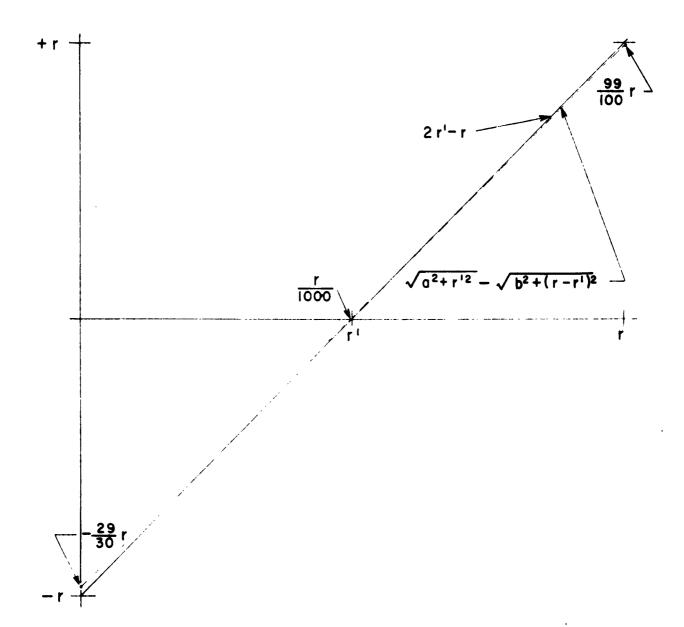
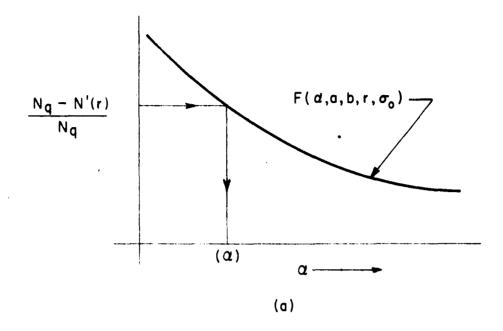
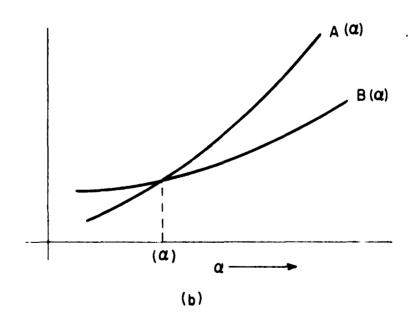


Figure 3
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